

# Force Field Development for Molecular Simulations with Structure Optimized Potential Refinement

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Recent Advances in Molecular Simulation Methods



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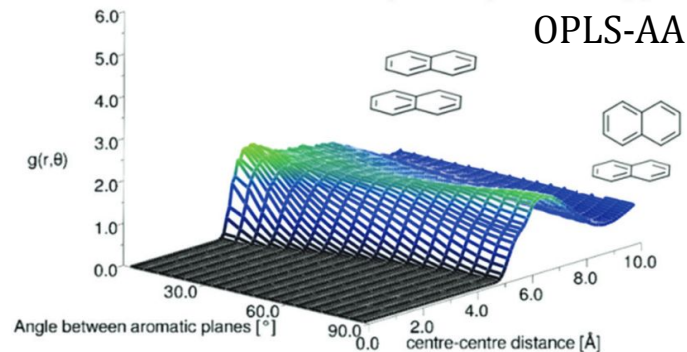
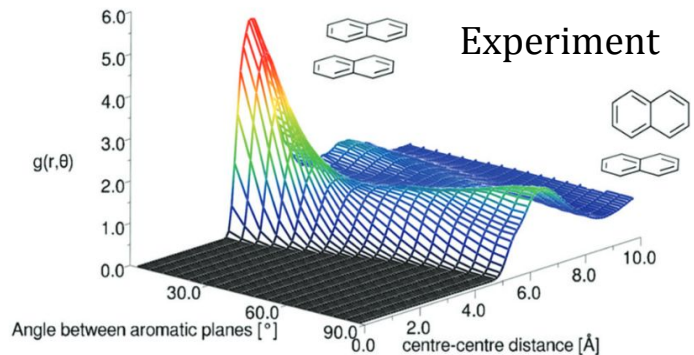


# Force Fields in Classical Molecular Dynamics

- Classical molecular simulation is ubiquitous across chemical physics.
- It is well established that classical methods overfit to the experimental data the force field is trained on.
- From statistical mechanics, we know that we can recover all thermodynamic properties of a system if we know both the structure and potential energy.

## Poor Structure Prediction in Naphthalene

Headen, 2019 *Phys. Chem. Chem. Phys.*

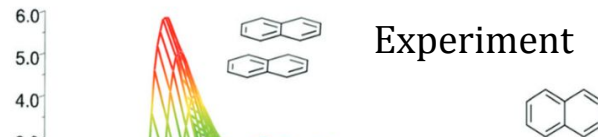


# Force Fields in Classical Molecular Dynamics

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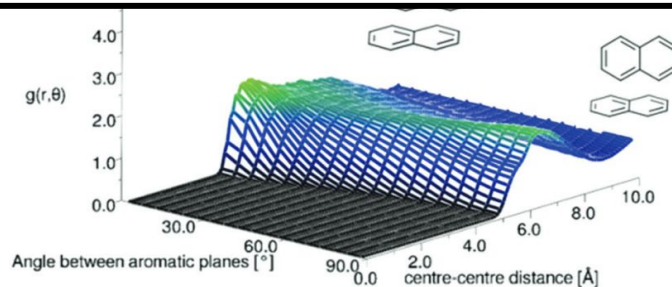
## Poor Structure Prediction in Naphthalene

Headen, 2019 *Phys. Chem. Chem. Phys.*



**What is preventing classical molecular models from simultaneously predicting structural and thermodynamic properties?**

thermodynamic properties of a system if we know both the structure and potential energy.



# Assumptions in classical force fields limit their accuracy

Pairwise Additive  
Approximation

$$U(\mathbf{r}) = \underbrace{\sum_i^N v_1(\mathbf{r}_i)}_{\text{external field}} + \underbrace{\sum_{i=1}^N \sum_{j \neq i}^N v_2(\mathbf{r}_{ij})}_{\text{two-body}} + \underbrace{\sum_i^N \sum_{j \neq i}^N \sum_{k \neq j}^N v_3(\mathbf{r}_{ijk}) + \dots}_{\text{many-body}}$$

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Pairwise Additive Approximation

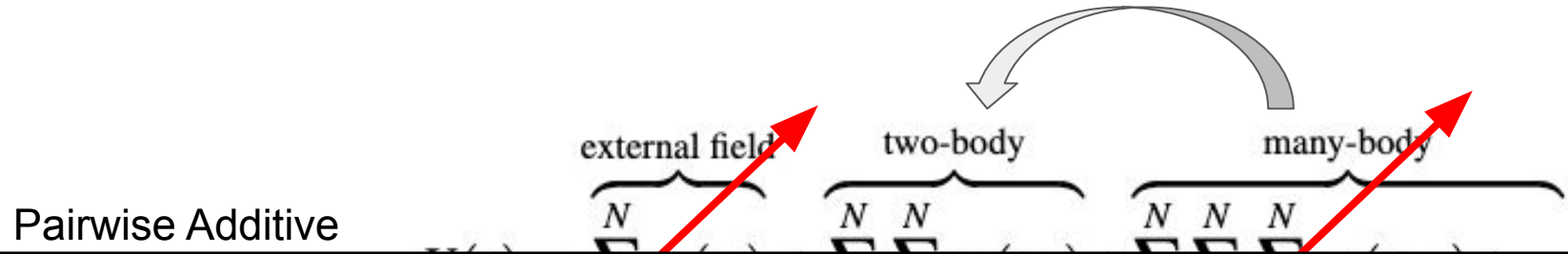
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Mie Intermolecular Potential

Effective pair potentials are fit to empirical forms

$$u_2^{\text{Mie}}(r) = \frac{\lambda}{\lambda - 6} \left(\frac{\lambda}{6}\right)^{6/\lambda - 6} \epsilon \left[ \left(\frac{\sigma}{r}\right)^\lambda - \left(\frac{\sigma}{r}\right)^6 \right]$$

# Assumptions in classical force fields limit their accuracy



**Can we model the potential energy and structure “accurately enough” to recover fluid thermodynamics from a purely classical model?**

Effective pair potentials are fit to empirical forms

$$v_2^{\text{Mie}}(r) = \frac{\lambda}{\lambda - 6} \left(\frac{\lambda}{6}\right)^{6/\lambda - 6} \epsilon \left[ \left(\frac{\sigma}{r}\right)^\lambda - \left(\frac{\sigma}{r}\right)^6 \right]$$

# The Henderson Inverse Theorem and Iterative Boltzmann Inversion

## Henderson's Theorem

If two systems are described by a pairwise additive Hamiltonian and have the same RDF, then their pair interaction term differs at most by a trivial constant.

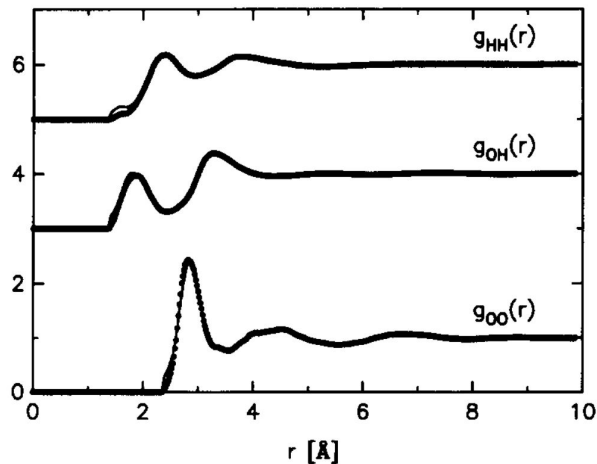
# The Henderson Inverse Theorem and Iterative Boltzmann Inversion

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### Neutron Scattering Analysis

Soper, 1996 *Chem. Phys.*





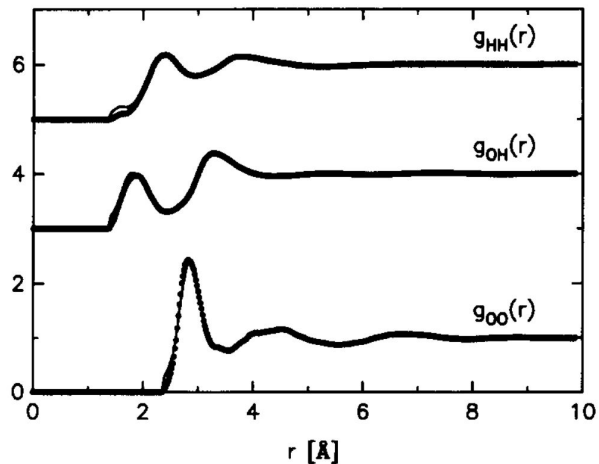
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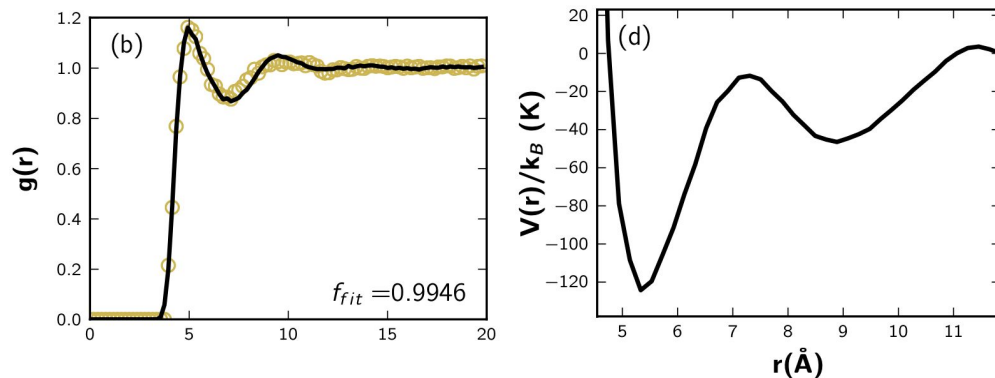
### Neutron Scattering Analysis

Soper, 1996 *Chem. Phys.*



### Coarse-Graining with Iterative Boltzmann Inversion

Moore, 2014 *J. Chem. Phys.*

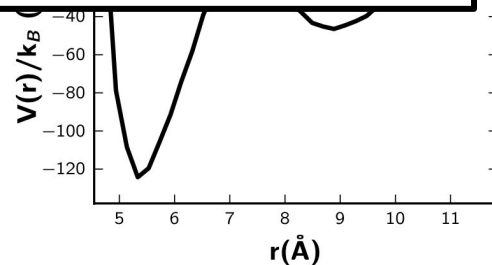
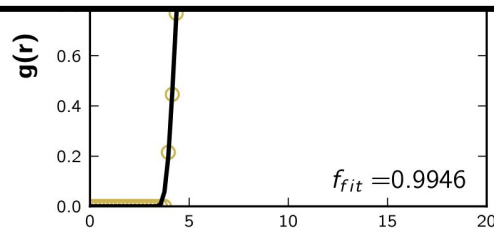
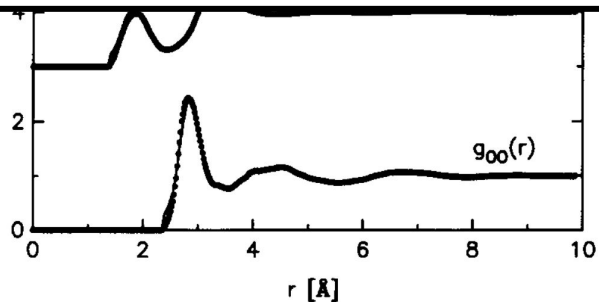


# The Henderson Inverse Theorem and Iterative Boltzmann Inversion

## Henderson's Theorem

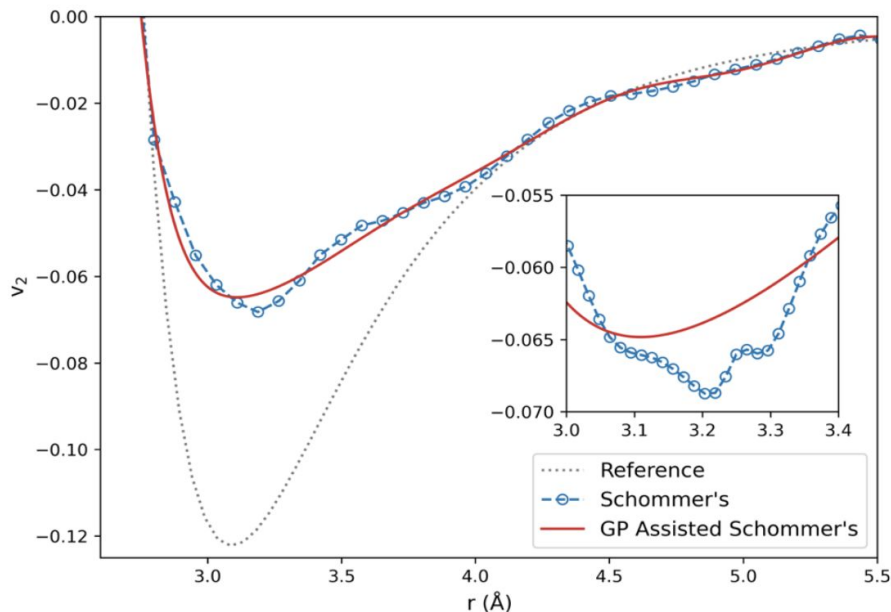
If two systems are described by a pairwise additive Hamiltonian and have the same RDF, then their pair interaction term differs at most by a trivial constant.

**Neutron scattering analysis methods (EPSR) and Iterative Boltzmann Inversion have not been shown to give accurate potentials in real fluids.**



# Structure Optimized Potential Refinement - A Physics-Guided, Probabilistic Iterative Boltzmann Inversion

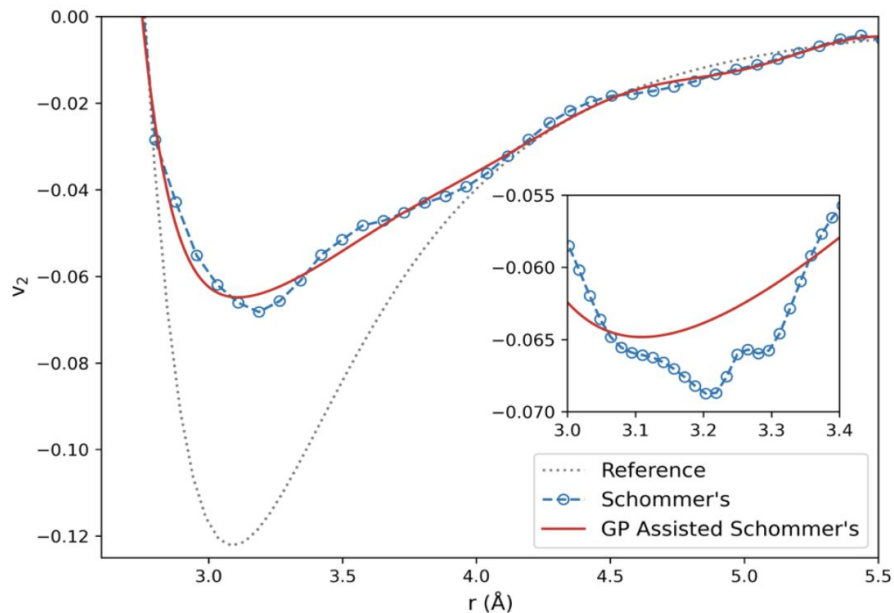
## Probabilistic Regression w/ GPs



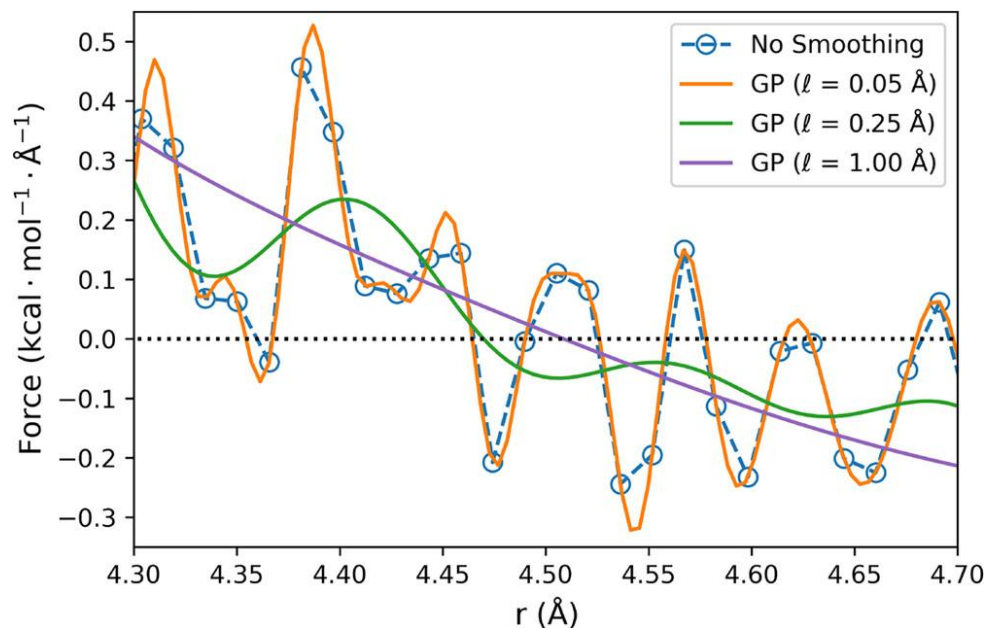
**Structure Optimized Potential Refinement**  
B. L. Shanks 2022, *J. Phys. Chem. Lett.*

# Structure Optimized Potential Refinement - A Physics-Guided, Probabilistic Iterative Boltzmann Inversion

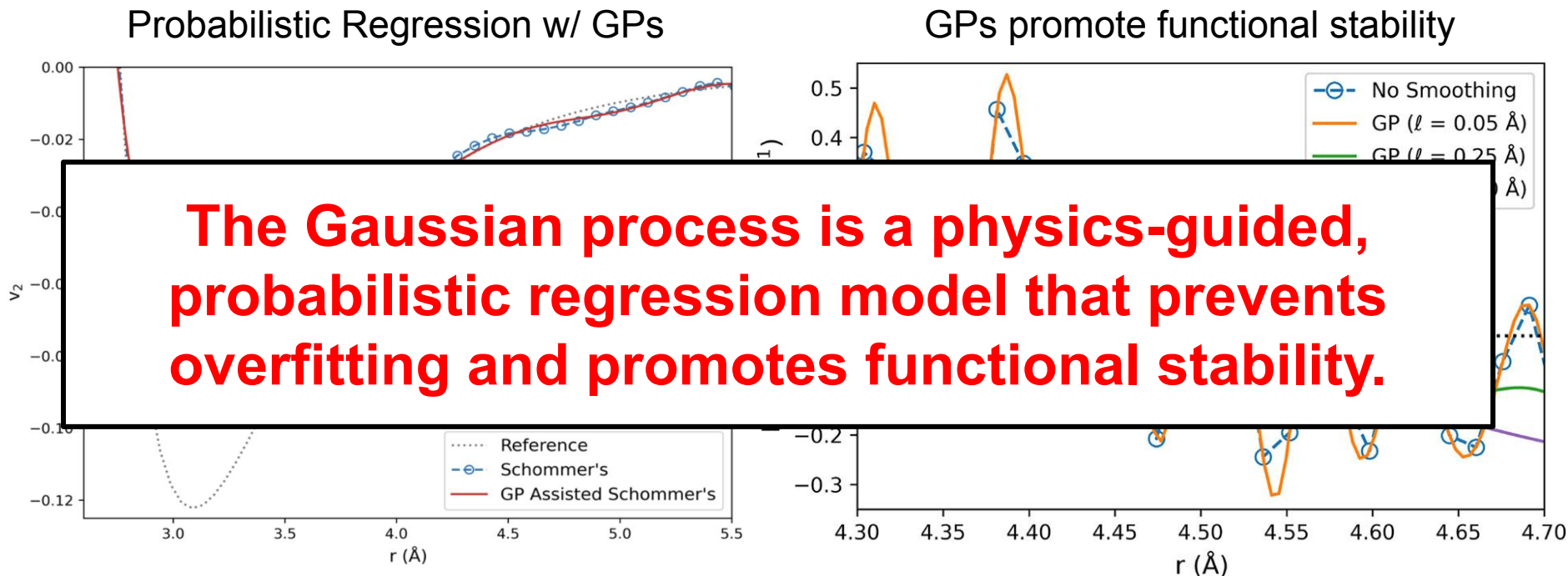
## Probabilistic Regression w/ GPs



## GPs promote functional stability

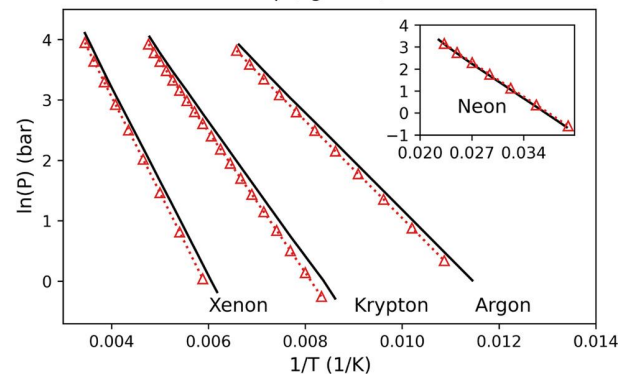
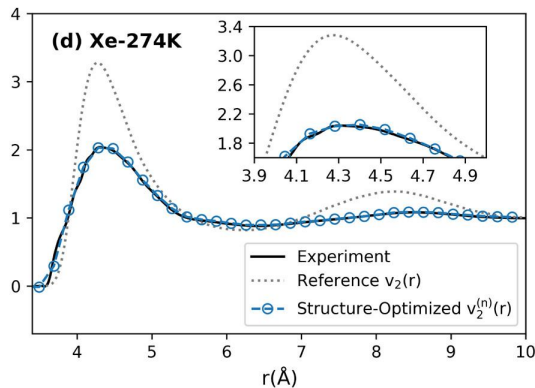
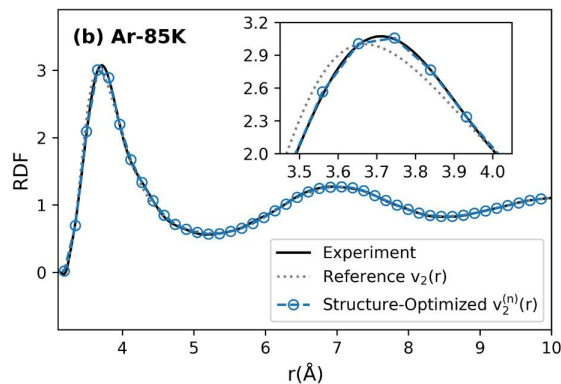
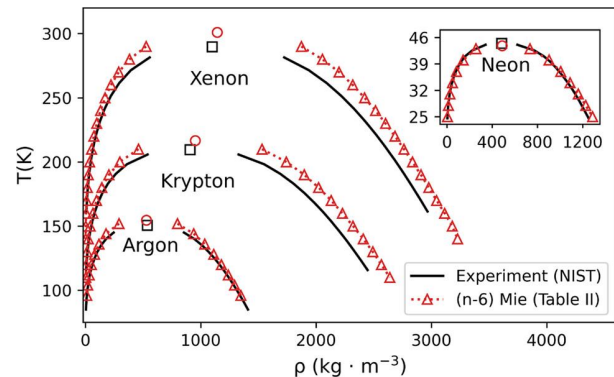
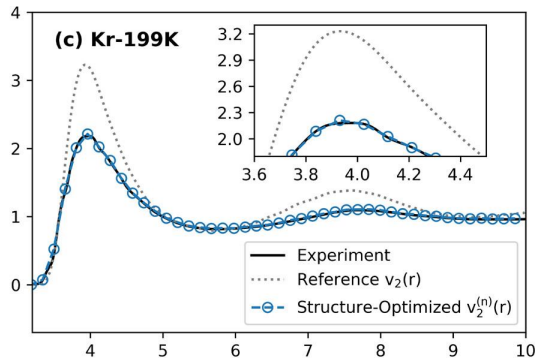
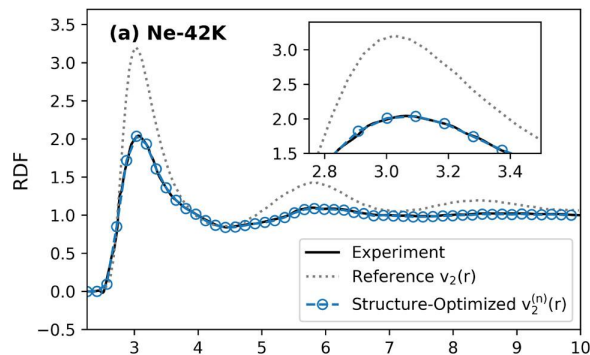


# Structure Optimized Potential Refinement - A Physics-Guided, Probabilistic Iterative Boltzmann Inversion



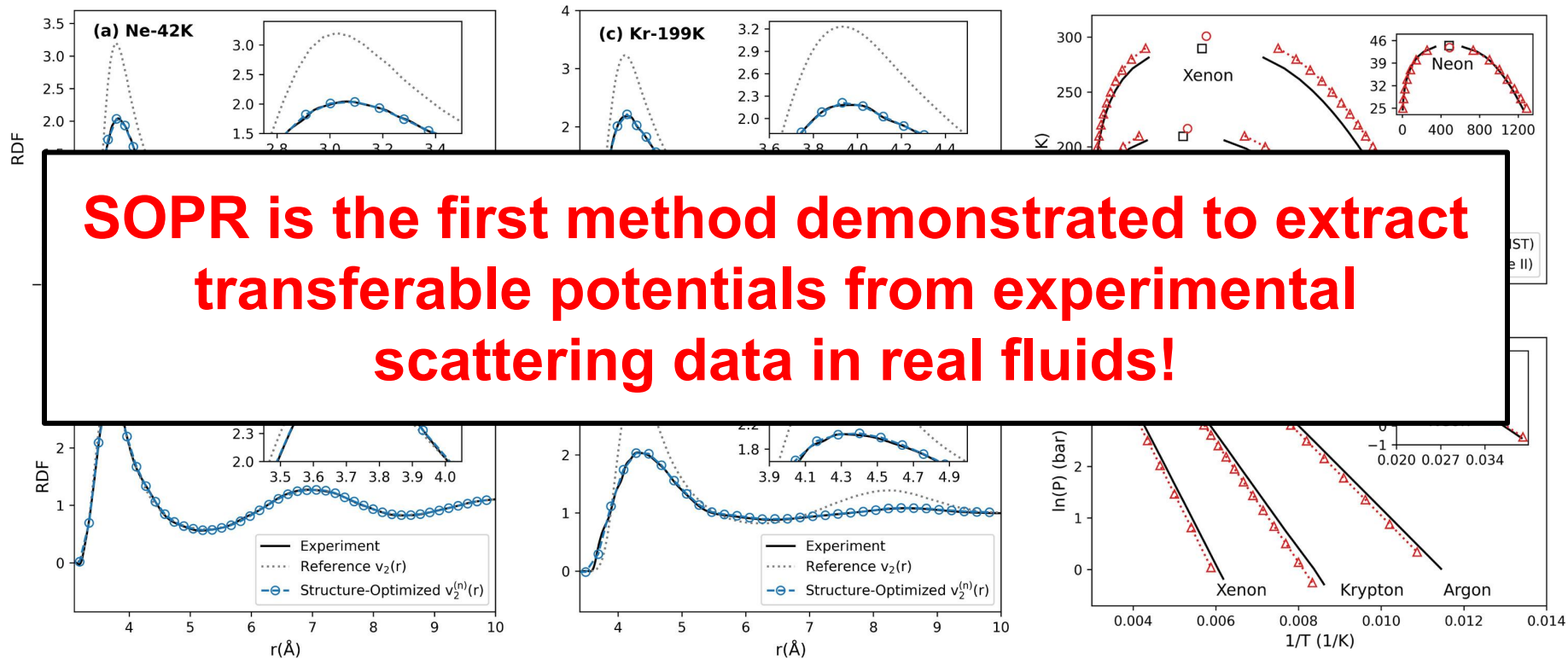
# Noble Gas Force Fields from Scattering Data

Radial Distribution Functions and Vapor Liquid Equilibrium Match with Excellent Agreement



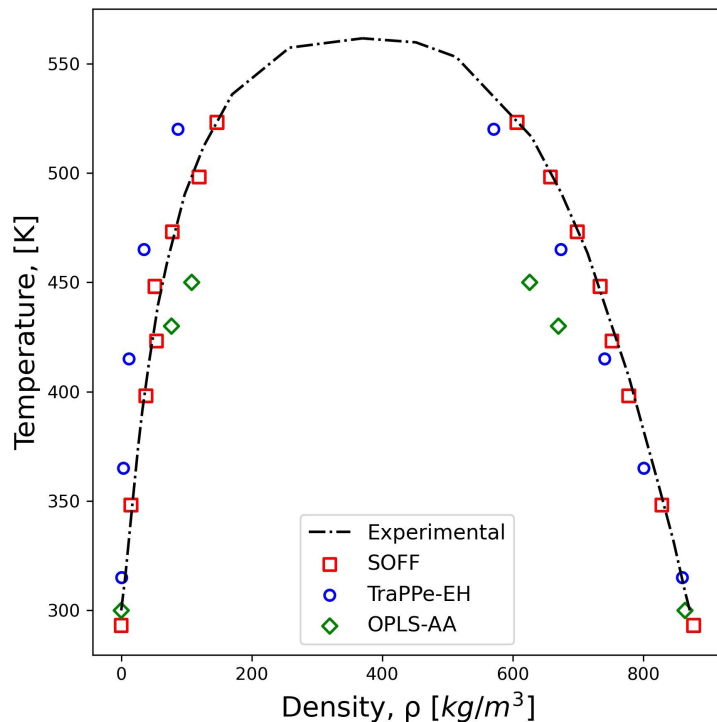
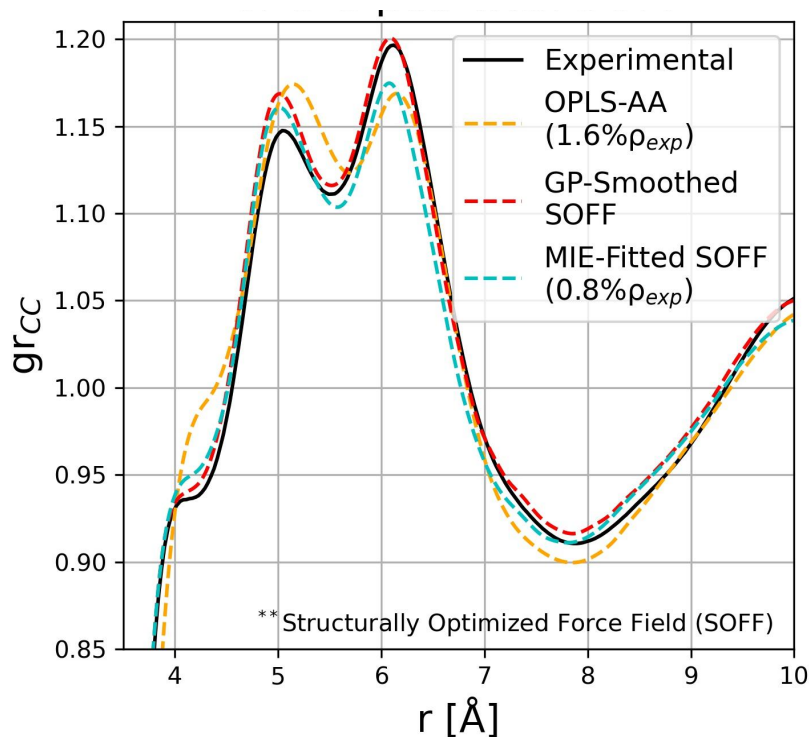
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Radial Distribution Functions and Vapor Liquid Equilibrium Match with Excellent Agreement



# Current and Future Work - Extending SOPR Beyond Simple Liquids

## Excellent RDF + VLE Agreement for Water, Benzene and Methane



Abdur Shazed



Harry Sullivan



# Summary and Key Takeaways

- SOPR is the first validated method to determine transferable potentials from experimental scattering data.
- Excellent performance on structure and vapor-equilibria in single atom and molecular liquids.
- Probabilistic machine learning techniques continue to shine for complex and indeterministic physical modeling.